Abstract. The intensity of copper X-radiation has been scrutinized as a function of the Bragg angle, employing both LiF and KBr crystals. X-ray intensity spectra were recorded for Cu as a function of Bragg angle using LiF, KBr single crystals using a PHYWE X-Ray Expert Unit (35 kV, 1 mA) with an X-ray goniometer, Plug-in Cu X-ray tube and a 2.2 mm diameter aperture tube. The scanning range was chosen to be 4°-55° for LiF and 3°-75° for KBr. The resultant spectra furnish a comprehensive portrayal of the variation in X-ray emission intensity relative to alterations in the Bragg angle. This investigation contributes to our comprehension of crystallographic phenomena and underscores the efficacy of diverse crystalline materials in X-ray diffraction studies. Precise determinations of the energy levels for characteristic copper X-ray lines have been obtained, revealing \( E(\text{K}\beta) = 8868.374 \pm 30.474 \text{ eV} \) and \( E(\text{K}\alpha) = 8026.349 \pm 31.634 \text{ eV} \). These findings accentuate the significance of X-ray spectroscopy in delineating the elemental composition and structural attributes of materials, while also affirming the role of theoretical predictions in elucidating experimental observations. Keywords: X-ray spectroscopy, Bragg angle, copper X-radiation, crystallographic phenomena, energy determination.

1. Introduction

Undoubtedly, X-ray diffraction stands as the cornerstone of solid-state physics and chemistry, representing the most pivotal and extensively utilized technique within these fields. X-ray generation stemming from collisions between protons or light ions and atoms stands as a pivotal area of investigation for understanding inner-shell ionization mechanisms. This subject has undergone extensive examination from experimental and theoretical standpoints over recent decades, yielding significant insights. Notably, extensive collections of experimental X-ray cross-section data have been assembled for K and L shells ionized by protons and helium ions, enabling meticulous comparisons with established theoretical models [1–5].

When high-energy electrons collide with the metallic anode within an X-ray tube, they generate X-rays characterized by a continuous energy spectrum. Embedded within this continuum are specific X-ray lines, known as characteristic X-ray lines, which remain independent of the anode voltage and are unique to the composition of the anode material. These lines originate from the ionization of an anode atom's K shell when struck by an electron. Subsequently, the resulting vacancy within the shell is filled by an electron transitioning from a higher energy level. The energy liberated during this de-excitation process manifests as an X-ray emission distinct to the anode atom.

X-ray spectroscopy serves as a pivotal tool in the realm of material characterization, offering unparalleled insights into the elemental composition and structural properties of diverse substances. The analysis of X-ray emission intensity as a function of the Bragg angle, facilitated by crystals such as LiF and KBr, constitutes a fundamental aspect of X-ray diffraction studies [6–8]. This investigation aims to elucidate the intricate relationship between Bragg angle variations and copper X-radiation intensity, thereby advancing our understanding of crystallographic phenomena. Additionally, precise determinations of energy levels for characteristic copper X-ray lines further underscore the utility of X-ray spectroscopy in unraveling the intricacies of material properties. By combining experimental
observations with theoretical predictions, this study endeavors to provide a comprehensive framework for interpreting X-ray diffraction data and exploring the structural characteristics of materials at the atomic level [9-10].

The aim of this article is to explore and elucidate the phenomenon of X-ray production resulting from collisions between protons or other light ions and atoms. By examining this process from both experimental and theoretical perspectives, the article seeks to enhance our understanding of inner-shell ionization mechanisms. Additionally, it aims to provide detailed comparisons between experimental X-ray cross-section data and existing theoretical models, thereby advancing the current understanding of X-ray generation in such collisions.

2. Methods

The X-ray intensity spectra have been recorded for copper as a function of Bragg angle using mounted LiF, KBr single crystals. X-ray spectra were recorded using a PHYWE X-Ray Expert Unit (35 kV, 1mA) with X-ray goniometer, X-ray Plug-in Cu tube and Diaphragm tube with the diameter of 2.2 mm (Figure 1). An X-ray tube with a copper anode generates X-radiation that is selected with the aid of a mounted crystal (LiF and KBr) as a function of the Bragg angle. A Geiger-Muller counter tube with the size of 15 mm measures the intensity of the radiation. The glancing angles of the characteristic X-ray lines are then used to determine the energy. The spectra were scanned in the range 4°-55° for LiF and 3°-75° for KBr with the gate time of 2 s and angle step width 0.1° using a XR 4.0 Software. The goniometer has been programmed for automatic calibration to obtain accurate reflection angles.

Set of mounted LiF and KBr crystals were purchased at the PHYWE Company with crystallographic orientation of 100. All crystals were 1 mm thick and had a usable surface area of 10 x 12 mm. The lattice spacing was 201.4 pm for the LiF crystal and 329 pm for KBr. There are also differences in the treated surface of the crystals, LiF has undergone polishing while KBr has not. All crystals used are assumed to be pure without any impurities.

3. Results and Discussion

As is known, when high-energy electrons hit the metal anode of an X-ray tube, X-rays with a continuum energy distribution are produced. We have analyzed polychromatic X-rays using LiF and KBr crystals (Figure 2–3).
Figure 2 presents copper X-ray intensity spectra recorded in range of 4°-55° for LiF crystals. The curve has a distinct peaks overlaying the continuous spectrum of the bremsstrahlung. The positions of these peaks remain consistent regardless of fluctuations in the anode voltage, suggesting their characteristic nature as copper lines. The initial set of lines corresponds to the first order of diffraction \((n = 1)\), whereas the subsequent set corresponds to \(n = 2\). This arises from the condition where X-rays of wavelength \(\lambda\) approach the crystal at an angle \(\nu\), leading to constructive interference post-scattering only when the path difference \(\delta\) between the partial waves reflected from the lattice planes equals one or more wavelengths.

Substituting the LiF crystal with a KBr crystal in the examination of the copper X-ray spectrum permits Bragg scatterings up to the fourth order of diffraction \((n = 4)\) as illustrated in Figure 3. The supplementary patterns observed beyond those depicted in Figure 3 stem from the increased
lattice constant of the KBr crystal. The maximums recorded during X-ray irradiation in range of 3°-75° also refer to characteristic copper peaks.

The bremsstrahlung spectrum depicted in Figure 3 exhibits a significant decrease in intensity towards smaller angles, notably at 8.0° and 16.3°. This decline aligns precisely with the theoretically anticipated bromide K absorption edge ($E_K = 13.474$ keV) within the first and second orders of diffraction. However, the potassium, lithium, and fluorine K absorption edges remain undetectable due to the bremsstrahlung spectrum's insufficient intensity within these energy ranges.

In pursuit of discerning the energy values associated with the characteristic X-ray emission of copper, and subsequently conducting a comparative analysis with those determined through the corresponding energy level diagram, our approach involved the utilization of the dataset delineated in Table 1.

### Table 1 – Obtained experimental data of alkali halide crystals

<table>
<thead>
<tr>
<th>Crystals</th>
<th>Initiation, deg</th>
<th>Maximum, deg</th>
<th>Shift, deg</th>
<th>Height, no/s</th>
<th>Area, no/s²</th>
</tr>
</thead>
<tbody>
<tr>
<td>LiF</td>
<td>19.8</td>
<td>20.5</td>
<td>20.8</td>
<td>3220.0</td>
<td>1022.0</td>
</tr>
<tr>
<td></td>
<td>22.1</td>
<td>22.8</td>
<td>23.2</td>
<td>9355.1</td>
<td>3123.4</td>
</tr>
<tr>
<td></td>
<td>43.7</td>
<td>44.0</td>
<td>44.1</td>
<td>405.11</td>
<td>102.5</td>
</tr>
<tr>
<td></td>
<td>49.7</td>
<td>50.2</td>
<td>50.5</td>
<td>1624.2</td>
<td>567.8</td>
</tr>
<tr>
<td></td>
<td>8.0</td>
<td>12.4</td>
<td>12.8</td>
<td>2110.3</td>
<td>1302.1</td>
</tr>
<tr>
<td></td>
<td>13.2</td>
<td>13.3</td>
<td>14.2</td>
<td>7043.4</td>
<td>2209.2</td>
</tr>
<tr>
<td></td>
<td>24.9</td>
<td>25.2</td>
<td>25.2</td>
<td>468.12</td>
<td>141.25</td>
</tr>
<tr>
<td>KBr</td>
<td>27.2</td>
<td>28.1</td>
<td>28.4</td>
<td>1798.3</td>
<td>554.62</td>
</tr>
<tr>
<td></td>
<td>39.3</td>
<td>39.5</td>
<td>39.3</td>
<td>128.21</td>
<td>39.83</td>
</tr>
<tr>
<td></td>
<td>44.1</td>
<td>44.7</td>
<td>45.1</td>
<td>419.01</td>
<td>149.14</td>
</tr>
<tr>
<td></td>
<td>68.6</td>
<td>69.2</td>
<td>69.2</td>
<td>235.31</td>
<td>71.23</td>
</tr>
</tbody>
</table>

### Table 2 – The calculated energy values pertaining to the characteristic copper X-ray lines

<table>
<thead>
<tr>
<th>Crystals</th>
<th>Level</th>
<th>$\nu/\nu$, deg</th>
<th>Line</th>
<th>$E_{\text{exp}}$, keV</th>
</tr>
</thead>
<tbody>
<tr>
<td>LiF</td>
<td>n = 1</td>
<td>20.3</td>
<td>$K_\beta$</td>
<td>8831.201</td>
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<tr>
<td></td>
<td></td>
<td>22.6</td>
<td>$K_\alpha$</td>
<td>7975.936</td>
</tr>
<tr>
<td></td>
<td>n = 2</td>
<td>43.8</td>
<td>$K_\beta$</td>
<td>8877.862</td>
</tr>
<tr>
<td></td>
<td></td>
<td>50.2</td>
<td>$K_\alpha$</td>
<td>8024.243</td>
</tr>
<tr>
<td></td>
<td>n = 1</td>
<td>12.2</td>
<td>$K_\beta$</td>
<td>8844.761</td>
</tr>
<tr>
<td></td>
<td></td>
<td>13.7</td>
<td>$K_\alpha$</td>
<td>8013.031</td>
</tr>
<tr>
<td></td>
<td>n = 2</td>
<td>25.2</td>
<td>$K_\beta$</td>
<td>8883.512</td>
</tr>
<tr>
<td>KBr</td>
<td>n = 1</td>
<td>28.1</td>
<td>$K_\alpha$</td>
<td>8025.795</td>
</tr>
<tr>
<td></td>
<td>n = 3</td>
<td>39.5</td>
<td>$K_\beta$</td>
<td>8904.498</td>
</tr>
<tr>
<td></td>
<td>n = 4</td>
<td>44.7</td>
<td>$K_\alpha$</td>
<td>8051.154</td>
</tr>
<tr>
<td></td>
<td>n = 4</td>
<td>69.3</td>
<td>$K_\beta$</td>
<td>8067.587</td>
</tr>
</tbody>
</table>

### 4. Conclusions

The intensity of copper X-radiation has been analyzed as a function of the Bragg angle, utilizing both LiF and KBr crystals. The observed spectra offer a comprehensive depiction of how the intensity of X-ray emissions varies with changes in the Bragg angle, thereby contributing to our understanding of crystallographic phenomena and the utility of different crystalline materials in X-ray diffraction studies.

Furthermore, the calculated energy values for the characteristic copper X-ray lines yield $E (K\beta) = 8868.374 \pm 30.474$ eV and $(K\alpha) = 8026.349 \pm 31.634$ eV, providing precise determinations...
for these energy levels. These findings underscore the utility of X-ray spectroscopy in elucidating the elemental composition and structural characteristics of materials, while also highlighting the efficacy of theoretical predictions in interpreting experimental observations.

References


Information about author:

Dias Sagatov – Research Assistant, Laboratory of Energy Storage Systems, National Laboratory Astana, 53 Kabanbay ave., Astana, Kazakhstan, dias.sagatov@list.ru

Author Contributions:

Dias Sagatov – concept, methodology, resources, data collection, testing, modeling, analysis, visualization, interpretation, drafting, editing, funding acquisition.

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